

Figure 1. An unweighted directed graph G

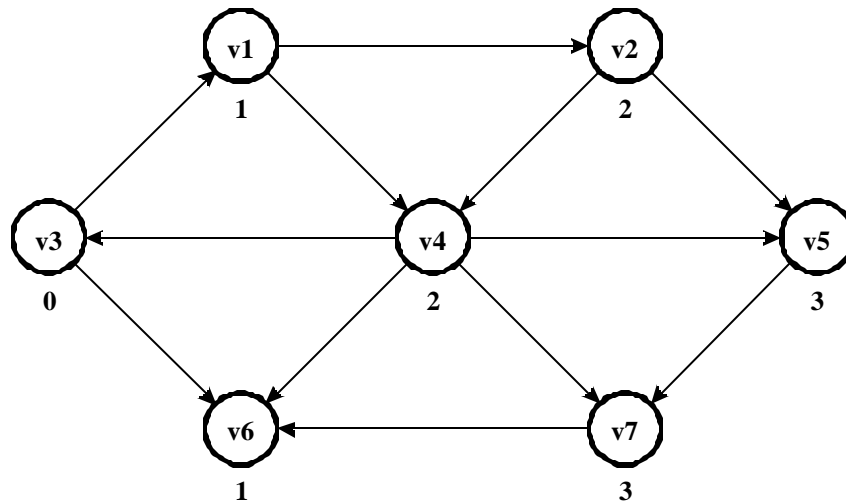


Figure 2. Final shortest paths from vertex  $v_3$  to every other vertex

| v              | After initialization          |      |                | v <sub>3</sub> dequeued       |      |                | v <sub>1</sub> dequeued                      |      |                |
|----------------|-------------------------------|------|----------------|-------------------------------|------|----------------|--|------|----------------|
|                | known                         | dist | path           | known                         | dist | path           | known  | dist | path           |
| v <sub>1</sub> | no                            | BIG  | -              | no                            | 1    | v <sub>3</sub> | yes  | 1    | v <sub>3</sub> |
| v <sub>2</sub> | no                            | BIG  | -              | no                            | BIG  | -              | no   | 2    | v <sub>1</sub> |
| v <sub>3</sub> | no                            | 0    | -              | yes                           | 0    | 0              | yes  | 0    | 0              |
| v <sub>4</sub> | no                            | BIG  | -              | no                            | BIG  | -              | no   | 2    | v <sub>1</sub> |
| v <sub>5</sub> | no                            | BIG  | -              | no                            | BIG  | -              | no   | BIG  | -              |
| v <sub>6</sub> | no                            | BIG  | -              | no                            | 1    | v <sub>3</sub> | no   | 1    | v <sub>3</sub> |
| v <sub>7</sub> | no                            | BIG  | -              | no                            | BIG  | -              | no   | BIG  | -              |
| q              | v <sub>3</sub>                |      |                | v <sub>1</sub> v <sub>6</sub> |      |                | v <sub>6</sub> v <sub>2</sub> v <sub>4</sub> |      |                |
| v              | v <sub>6</sub> dequeued       |      |                | v <sub>2</sub> dequeued       |      |                | v <sub>4</sub> dequeued                      |      |                |
|                | known                         | dist | path           | known                         | dist | path           | known  | dist | path           |
| v <sub>1</sub> | yes                           | 1    | v <sub>3</sub> | yes                           | 1    | v <sub>3</sub> | yes  | 1    | v <sub>3</sub> |
| v <sub>2</sub> | no                            | 2    | v <sub>1</sub> | yes                           | 2    | v <sub>1</sub> | yes  | 2    | v <sub>1</sub> |
| v <sub>3</sub> | yes                           | 0    | 0              | yes                           | 0    | 0              | yes  | 0    | 0              |
| v <sub>4</sub> | no                            | 2    | v <sub>1</sub> | no                            | 2    | v <sub>1</sub> | yes  | 2    | v <sub>1</sub> |
| v <sub>5</sub> | no                            | BIG  | -              | no                            | 3    | v <sub>2</sub> | no   | 3    | v <sub>2</sub> |
| v <sub>6</sub> | yes                           | 1    | v <sub>3</sub> | yes                           | 1    | v <sub>3</sub> | yes  | 1    | v <sub>3</sub> |
| v <sub>7</sub> | no                            | BIG  | -              | no                            | BIG  | -              | no   | 3    | v <sub>4</sub> |
| q              | v <sub>2</sub> v <sub>4</sub> |      |                | v <sub>4</sub> v <sub>5</sub> |      |                | v <sub>5</sub> v <sub>7</sub>                |      |                |
| v              | v <sub>5</sub> dequeued       |      |                | v <sub>7</sub> dequeued       |      |                |  |      |                |
|                | known                         | dist | path           | known                         | dist | path           |  |      |                |
| v <sub>1</sub> | yes                           | 1    | v <sub>3</sub> | yes                           | 1    | v <sub>3</sub> |  |      |                |
| v <sub>2</sub> | yes                           | 2    | v <sub>1</sub> | yes                           | 2    | v <sub>1</sub> |  |      |                |
| v <sub>3</sub> | yes                           | 0    | 0              | yes                           | 0    | 0              |  |      |                |
| v <sub>4</sub> | yes                           | 2    | v <sub>1</sub> | yes                           | 2    | v <sub>1</sub> |  |      |                |
| v <sub>5</sub> | yes                           | 3    | v <sub>2</sub> | yes                           | 3    | v <sub>2</sub> |  |      |                |
| v <sub>6</sub> | yes                           | 1    | v <sub>3</sub> | yes                           | 1    | v <sub>3</sub> |  |      |                |
| v <sub>7</sub> | no                            | 3    | v <sub>4</sub> | yes                           | 3    | v <sub>4</sub> |  |      |                |
| q              | v <sub>7</sub>                |      |                | empty                         |      |                |  |      |                |

**Unweighted shortest path algorithm:**

1. Create queue  $Q$ , allocating as many entries in the queue as there are vertices in the graph.
2. Initialize table  $T$  making the input vertex  $V$  the origin.
3. Insert origin vertex  $V_o$  into the queue.
4. **While** queue  $Q$  is not empty
  - 4.1. Remove vertex  $V$  from the queue.
  - 4.2. Mark vertex  $V$  as "known."
  - 4.3. For each vertex  $W$  adjacent to  $V$  do
    - 4.3.1. **If** the distance to vertex  $W$  is undefined ( $BIG$ ) then
      - 4.3.1.1. Add one to the distance to vertex  $V$  and assign that value to vertex  $W$  in table  $T$ .
      - 4.3.1.2. Assign vertex  $V$  to the path to vertex  $W$ .
      - 4.3.1.3. Insert vertex  $W$  into the queue.
5. **end while**