

1. Heapsort is divided into two steps.
  - 1.1. Insert all the values into a heap.
  - 1.2. Remove all the values from the heap and store them in sequence in an array.
2. Inserting a single value on heap requires  $\log_2 n + 1$  operations. Recall that the number of operations required to insert a value on the heap is a function of the number of nodes in the path defined by the height,  $h$ , of the heap.  $h = \lfloor \log_2 n \rfloor$  where  $n$  is the number of values stored in the heap. The number of nodes in the path from a leaf to the root is always one more than the height. Thus, the number of operations,  $T(n)$ , required to insert a single value is,  $T(n) = cf(\log_2 n + 1)$ .
3. The cost of inserting all the values,  $n$ , is the product of inserting a single value  $n$  times. Since the heap grows with the insertion of each value, the cost of inserting each value is no greater than inserting the last value.  $T(n) = cf(n + n \log_2 n)$ .
4. The cost of removing all the values is the same as inserting all the values.  
 $T(n) = cf(2n + 2n \log_2 n) \Rightarrow T(n) = O(n \log_2 n)$