6. Data Types

6.1. Introduction

<table>
<thead>
<tr>
<th>Data Type</th>
<th>A data type defines a collection of data values and a set of predefined operations on those values.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Descriptor</td>
<td>A descriptor is the collection of the attributes of a variable. If the attributes are all static, descriptors are required only at compile time. Descriptors are built by the compiler, usually as a part of the symbol table.</td>
</tr>
<tr>
<td>Object</td>
<td>An object is an instance of a user-defined abstract data type.</td>
</tr>
</tbody>
</table>

6.2. Primitive Data Types

<table>
<thead>
<tr>
<th>Primitive Data Type</th>
<th>Data types that are not defined in terms of other types are called primitive data types.</th>
</tr>
</thead>
</table>

6.2.1. Numeric Types

6.2.1.1. Integer

Definition: An integer is a number without a fractional part. The set of integers is the union of the set of whole numbers and the set of negative counting numbers.

Integers and whole numbers. C++ implements both integers (signed) and whole numbers (unsigned).

Ranges: The range of values a particular integer variable can take on is limited by the number of bits allocated to that variable. The type-specifiers `char`, `short`, `int`, and `long` define the relative range of values that a variable of that type can take on.

\[ \text{char} \leq \text{short} \leq \text{int} \leq \text{long} \]

Implementation: Integers are implemented as two's complement binary integers. Whole numbers are implemented as unsigned binary integers. Several field widths (`w`) are common including 8, 16, 32, and 64 bits.

Integers: Let \( \mathbb{Z} \) be the set of integers and \( I \) designate the set of integer types.

\[
I = \left\{ i \in \mathbb{Z} \mid -2^{w-1} \leq i \leq 2^{w-1} - 1, \; w \in \{8, 16, 32, 64\} \right\}
\]

- An 8-bit integer \( c \) ranges from \(-2^7 \leq c \leq 2^7 - 1\) or \(-128 \leq c \leq 127\)
- An 16-bit integer \( s \) ranges from \(-2^{15} \leq s \leq 2^{15} - 1\) or \(-32,768 \leq s \leq 32,767\)
- 32-bit integer \( i \) ranges from \(-2^{31} \leq i \leq 2^{31} - 1\) or \(-2,147,483,648 \leq i \leq 2,147,483,647\)
- A 64-bit integer \( l \) ranges from \(-2^{63} \leq l \leq 2^{63}\)
Let $U$ designate the set of unsigned integer types.

$$U = \{ u \in \mathbb{Z} | 0 \leq u \leq 2^n - 1, n \in \{8, 16, 32, 64\} \}$$

- An 8-bit whole number $c$ ranges from $0 \leq c \leq 2^8$ or $0 \leq c \leq 255$.
- A 16-bit integer $s$ ranges from $0 \leq s \leq 2^{16}$ or $0 \leq s \leq 65,535$.
- A 32-bit integer $i$ ranges from $0 \leq i \leq 2^{32}$ or $0 \leq i \leq 4,294,967,296$.
- A 64-bit integer $l$ ranges from $0 \leq l \leq 2^{64}$.

**Integers and whole numbers.** The relationship between integers and whole numbers for a given size is shown in Figure 1.

![Figure 1. Signed and unsigned integer values](image)

**Representation:** Implementation: Integers are implemented as two’s complement binary integers. Whole numbers are implemented as unsigned binary integers. Several field widths ($w$) are common including 8, 16, and 32 bits.

- **Figure 2.** 8-bit whole number representation `unsigned char uc=5;`
  
<table>
<thead>
<tr>
<th>Bit Position</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 0 0 0 0 1 0 1</td>
</tr>
</tbody>
</table>

- **Figure 3.** 8-bit integer representation `char sc=-5;`
  
<table>
<thead>
<tr>
<th>Bit Position</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 1 1 1 0 1 1</td>
</tr>
</tbody>
</table>

**6.2.1.2. Floating-Point**

**Definition:**

Real types simulate real numbers. Real types are discrete whereas the set of real numbers is continuous. Real types are called floating-point numbers. The density of floating-point numbers is shown on a real number line in Figure 1.

![Figure 4. Density of floating-point numbers](image)
Sets: Each set is dependent on its representation.

Figure 5. IEEE-754 single binary floating-point representation used to implement type float.

\[ R = \{ r \in \mathbb{R} \mid -1^s \times 2^{c-b} \times 1.f, s \in \{0,1\}, 1 \leq c \leq 254, b = 127, f = \sum_{k=1}^{23} f_k \times 2^{-k}, f_k \in \{0,1\} \} \]

Figure 6. IEEE-754 double binary floating-point representation used to implement type double.

\[ R = \{ r \in \mathbb{R} \mid -1^s \times 2^{c-b} \times 1.f, s \in \{0,1\}, 1 \leq c \leq 2047, b = 1023, f = \sum_{k=1}^{52} f_k \times 2^{-k}, f_k \in \{0,1\} \} \]
6.2.1.3. Complex

Fortran and Python support a primitive type of complex. A value of type complex is an ordered pair of floating-point values. The example below is from Python

\((7+3j)\)

6.2.1.4. Decimal

Computers designed for business systems applications often have support for decimal data types. COBOL, C#, and Visual Basic have decimal types.

Decimal types are stored very much like character strings, using binary codes for the decimal digits.

**BCD Code**

BCD codes were conceived to perform decimal arithmetic and are particularly useful where monetary values are represented. Banks and other financial institutions require that all monetary values be resolved to the nearest penny.

Four bits are used to represent each decimal digit leaving six unused codes as shown below.

<table>
<thead>
<tr>
<th>Decimal Symbol</th>
<th>BCD Digit</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0000</td>
</tr>
<tr>
<td>1</td>
<td>0001</td>
</tr>
<tr>
<td>2</td>
<td>0010</td>
</tr>
<tr>
<td>3</td>
<td>0011</td>
</tr>
<tr>
<td>4</td>
<td>0100</td>
</tr>
<tr>
<td>5</td>
<td>0101</td>
</tr>
<tr>
<td>6</td>
<td>0110</td>
</tr>
<tr>
<td>7</td>
<td>0111</td>
</tr>
<tr>
<td>8</td>
<td>1000</td>
</tr>
<tr>
<td>9</td>
<td>1001</td>
</tr>
</tbody>
</table>

Each decimal digit is represented by a group of four (4) bits. For example, \((185)_{10} = (0001 1000 0101)_{\text{BCD}}\).
6.2.2. Boolean Types
The set $B$ of Boolean values consist of two values $B = \{false, true\}$

Representation

\[
\begin{array}{cccccccc}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\
7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\
\end{array}
\]

Bit Position

Figure 7. Boolean data representation for constant true.

6.2.3. Character Types

Representation:
A variable of type char can store a single member from the set of ASCII (American Standard Code for Information Interchange).

A variable of type wchar_t can store a wide character occupying 16 bits.

Characters are integer codes. Let $C_8$ be the set of all characters represented by type char.

\[C_8 = \{c \in C_8 | 0 \leq c \leq 2^8 - 1\}\]

Let $C_{16}$ be the set of all characters represented by the type wchar_t.

\[C_{16} = \{c \in C_{16} | 0 \leq c \leq 2^{16} - 1\}\]

A character is distinguished from an integer only when it is printed or displayed. Instead of printing or displaying the integer code, the character face is printed or displayed.
<table>
<thead>
<tr>
<th>Decimal Code</th>
<th>ASCII Character</th>
<th>Decimal Code</th>
<th>ASCII Character</th>
<th>Decimal Code</th>
<th>ASCII Character</th>
<th>Decimal Code</th>
<th>ASCII Character</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>NUL</td>
<td>32</td>
<td>SP</td>
<td>64</td>
<td>`</td>
<td>96</td>
<td>`</td>
</tr>
<tr>
<td>1</td>
<td>SOH</td>
<td>33</td>
<td>!</td>
<td>65</td>
<td>A</td>
<td>97</td>
<td>a</td>
</tr>
<tr>
<td>2</td>
<td>STX</td>
<td>34</td>
<td>“</td>
<td>66</td>
<td>B</td>
<td>98</td>
<td>b</td>
</tr>
<tr>
<td>3</td>
<td>ETX</td>
<td>35</td>
<td>#</td>
<td>67</td>
<td>C</td>
<td>99</td>
<td>c</td>
</tr>
<tr>
<td>4</td>
<td>EOT</td>
<td>36</td>
<td>$</td>
<td>68</td>
<td>D</td>
<td>100</td>
<td>d</td>
</tr>
<tr>
<td>5</td>
<td>ENQ</td>
<td>37</td>
<td>%</td>
<td>69</td>
<td>E</td>
<td>101</td>
<td>e</td>
</tr>
<tr>
<td>6</td>
<td>ACK</td>
<td>38</td>
<td>&amp;</td>
<td>70</td>
<td>F</td>
<td>102</td>
<td>f</td>
</tr>
<tr>
<td>7</td>
<td>BEL</td>
<td>39</td>
<td>’</td>
<td>71</td>
<td>G</td>
<td>103</td>
<td>g</td>
</tr>
<tr>
<td>8</td>
<td>BS</td>
<td>40</td>
<td>(</td>
<td>72</td>
<td>H</td>
<td>104</td>
<td>h</td>
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<tr>
<td>9</td>
<td>HT</td>
<td>41</td>
<td>)</td>
<td>73</td>
<td>I</td>
<td>105</td>
<td>i</td>
</tr>
<tr>
<td>10</td>
<td>LF</td>
<td>42</td>
<td>*</td>
<td>74</td>
<td>J</td>
<td>106</td>
<td>j</td>
</tr>
<tr>
<td>11</td>
<td>VT</td>
<td>43</td>
<td>+</td>
<td>75</td>
<td>K</td>
<td>107</td>
<td>k</td>
</tr>
<tr>
<td>12</td>
<td>FF</td>
<td>44</td>
<td>,</td>
<td>76</td>
<td>L</td>
<td>108</td>
<td>l</td>
</tr>
<tr>
<td>13</td>
<td>CR</td>
<td>45</td>
<td>-</td>
<td>77</td>
<td>M</td>
<td>109</td>
<td>m</td>
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<tr>
<td>14</td>
<td>SO</td>
<td>46</td>
<td>.</td>
<td>78</td>
<td>N</td>
<td>110</td>
<td>n</td>
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<tr>
<td>15</td>
<td>SI</td>
<td>47</td>
<td>/</td>
<td>79</td>
<td>O</td>
<td>111</td>
<td>o</td>
</tr>
<tr>
<td>16</td>
<td>DLE</td>
<td>48</td>
<td>0</td>
<td>80</td>
<td>P</td>
<td>112</td>
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<tr>
<td>17</td>
<td>DC1</td>
<td>49</td>
<td>1</td>
<td>81</td>
<td>Q</td>
<td>113</td>
<td>q</td>
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<tr>
<td>18</td>
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<td>50</td>
<td>2</td>
<td>82</td>
<td>R</td>
<td>114</td>
<td>r</td>
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<tr>
<td>19</td>
<td>DC3</td>
<td>51</td>
<td>3</td>
<td>83</td>
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<td>115</td>
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</tr>
<tr>
<td>20</td>
<td>DC4</td>
<td>52</td>
<td>4</td>
<td>84</td>
<td>T</td>
<td>116</td>
<td>t</td>
</tr>
<tr>
<td>21</td>
<td>NAK</td>
<td>53</td>
<td>5</td>
<td>85</td>
<td>U</td>
<td>117</td>
<td>u</td>
</tr>
<tr>
<td>22</td>
<td>SYN</td>
<td>54</td>
<td>6</td>
<td>86</td>
<td>V</td>
<td>118</td>
<td>v</td>
</tr>
<tr>
<td>23</td>
<td>ETB</td>
<td>55</td>
<td>7</td>
<td>87</td>
<td>W</td>
<td>119</td>
<td>w</td>
</tr>
<tr>
<td>24</td>
<td>CAN</td>
<td>56</td>
<td>8</td>
<td>88</td>
<td>X</td>
<td>120</td>
<td>x</td>
</tr>
<tr>
<td>25</td>
<td>EM</td>
<td>57</td>
<td>9</td>
<td>89</td>
<td>Y</td>
<td>121</td>
<td>y</td>
</tr>
<tr>
<td>26</td>
<td>SUB</td>
<td>58</td>
<td>:</td>
<td>90</td>
<td>Z</td>
<td>122</td>
<td>z</td>
</tr>
<tr>
<td>27</td>
<td>ESC</td>
<td>59</td>
<td>;</td>
<td>91</td>
<td>]</td>
<td>123</td>
<td>{</td>
</tr>
<tr>
<td>28</td>
<td>FS</td>
<td>60</td>
<td>&lt;</td>
<td>92</td>
<td>\</td>
<td>124</td>
<td></td>
</tr>
<tr>
<td>29</td>
<td>GS</td>
<td>61</td>
<td>=</td>
<td>93</td>
<td>]</td>
<td>125</td>
<td>}</td>
</tr>
<tr>
<td>30</td>
<td>RS</td>
<td>62</td>
<td>&gt;</td>
<td>94</td>
<td>^</td>
<td>126</td>
<td>~</td>
</tr>
<tr>
<td>31</td>
<td>US</td>
<td>63</td>
<td>?</td>
<td>95</td>
<td>_</td>
<td>127</td>
<td>DEL</td>
</tr>
</tbody>
</table>

*Figure 8. ASCII Character Set*
<table>
<thead>
<tr>
<th>Coding</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ASCII</td>
<td>American Standard Code for Information Interchange 8-bit code 0 to 127</td>
</tr>
<tr>
<td>ISO 8859-1</td>
<td>International Standards Organization 8-bit code 0 to 255 Used by Ada 95</td>
</tr>
<tr>
<td>UCS-2</td>
<td>Unicode Consortium 16-bit code published in 1991 First 128 characters are identical to ASCII Java, JavaScript, Python, Perl, C#</td>
</tr>
</tbody>
</table>

6.3. Character String Types

A character string type is one in which the values consist of sequences of characters.

6.3.1. Design Issues

- Should strings be simply a special kind of character array or a primitive type?
- Should strings have static or dynamic length?

6.3.2. Strings and Their Operations

Operations

- assignment
- catenation
- substring reference
- comparison
- pattern matching

A substring reference is a reference to a substring of a given string.

Assignment and comparison operations on character strings are complicated by the possibility of string operands of different lengths. For example, what happens when a longer string is assigned to a shorter string or vice versa?

C uses char arrays to store character strings.

Representation:

A C-string is an array of characters terminated by a null character. For example, the string “toy” is represented as shown in figure 1.

Figure 9. C-string “toy”.

C

toy
**Declaration:**
A C-string is declared as an array of characters. Examples are given below.

```c
char s[10];    // s is an array of 10 characters having elements s[0] .. s[9].
                // s can hold up to 9 characters
char t[]="one";    // t is a string initialized to the characters ‘o’, ‘n’, ‘e’, ‘\0’
char u[3]="one";    // u is initialized to the characters ‘o’, ‘n’, ‘e’
                // u is not a string.
char v[]={‘o’,’n’,’e’,’\0’};  // v is a string having four (4) characters. Each character is initialized.
char e[]="";     // e is a string having a single character, the null terminator.
                // e is the empty string
```

**Strings and pointers to strings:**
1. Strings are referenced by pointers to the actual string. For example, variable \( t \), is used to reference string \( t \) declared as `char t[]=“toy”;
2. When the name of an array appears without a subscripting operator [], the type of the array name is changed to a pointer to the element type. For example, \( t \) has type `char*` because elements of \( t \) have type `char` and \( t \) is an array.
3. String pointers can be declared directly. For example, `char* s;`. Variable \( s \) can be assigned to point to a string but no such assignment has been made yet. Variable \( s \) is said to be undefined. References to \( s \) will likely cause an execution-time error.
4. A string pointer can be initialized. For example `char* s="toy";` Storage for string “toy” is allocated in the constant area of the program. The string “toy” cannot be changed. String \( s \), however, can be reassigned. Refer to figure 2.

![Figure 10. char* s="toy";](image-url)
### Operations:

```cpp
#include <string>
```

<table>
<thead>
<tr>
<th>Declaration</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>int <code>strlen</code></td>
<td>Function <code>strlen</code> returns the number of characters in the string referenced by parameter <code>s</code>. The terminating character is excluded from the count returned by function <code>strlen</code>.</td>
<td>char <code>s[]</code> = &quot;one&quot;; int <code>c = strlen(s); cout &lt;&lt; c;</code> Output 3</td>
</tr>
<tr>
<td>char* <code>strcpy</code></td>
<td>Function <code>strcpy</code> copies the contents of the string <code>s</code> to the string <code>d</code>, overwriting the contents of <code>d</code>. The entire contents of <code>s</code> are copied, plus the terminating null character even if <code>s</code> is longer than <code>d</code>. The argument <code>d</code> is returned.</td>
<td>char <code>d[]</code> = &quot;destination&quot;; char <code>s[]</code> = &quot;source&quot;; char* <code>t = strcpy(d, s);</code> cout &lt;&lt; <code>d</code>; Output source</td>
</tr>
<tr>
<td>char* <code>strcat</code></td>
<td>Function <code>strcat</code> appends the contents of string <code>s</code> to string <code>d</code>. A pointer to string <code>d</code> is returned. The null character that terminates <code>d</code> (and perhaps other characters following it in memory) is overwritten with characters from <code>s</code> and a new terminating null character. Characters are copied from <code>s</code> until a null character is encountered in <code>s</code>. The memory beginning with <code>d</code> is assumed to be large enough to hold both strings.</td>
<td>char <code>d[10]</code> = &quot;One&quot;; char <code>s[]</code> = &quot;, two&quot;; char* <code>t = strcat(d, s);</code> Output One, two</td>
</tr>
<tr>
<td>int <code>strcmp</code></td>
<td>Function <code>strcmp</code> lexicographically compares the contents of the null-terminated string <code>u</code> with the contents of the null-terminated string <code>v</code>. It returns a value of type <code>int</code> that is less than zero if <code>u &lt; v</code>; equal zero if <code>u = v</code>; and greater than zero if <code>u &gt; v</code>.</td>
<td>char <code>u[]</code> = &quot;ted&quot;; char <code>v[]</code> = &quot;tom&quot;; int <code>c = strcmp(u, v);</code> cout &lt;&lt; <code>c</code>; Output -1</td>
</tr>
</tbody>
</table>

Table 1. Selected functions in library `cstring` (`#include <cstring>`) continued
C++ strings

Representation:
The representation of C++ string is hidden.

Declaration:
Include file `#include <string>`. Use type name `string`. Review declarations below.

```cpp
string s; // s is a string.
string t="one"; // string t is initialized to the string “one”
string u="two"; // string u is initialized to the string “two”
string e=""; // string e is initialized to the empty string
```

Examples:
Program `p01` illustrates how to find the length of a string

```cpp
#include <iostream>
#include <string>
using namespace std;
int main()
{
    string s="toy";
    cout << "length(" << s << ")=" << s.length();
    cout << endl;
    return 0;
}
```

Figure 11. Program `p01`.

Program `p01` output.
```
length(toy)=3
```

Program `p02` illustrates string assignment.

```cpp
#include <iostream>
#include <string>
using namespace std;
int main()
{
    string s="source";
    string d="destination";
    d=s;
    cout << "d=" << d;
    cout << endl;
    return 0;
}
```

Figure 12. Program `p02`.

Program `p02` output.
```
d=source
```
Program p03 illustrates string concatenation.

```cpp
#include <iostream>
#include <string>
using namespace std;

int main()
{
    string s("");
    for (;;)
    {
        cout << endl;
        cout << "Enter a string. ";
        string t;
        cin >> t;
        if (cin.eof()) break;
        s=s+" ";
        s=s+t;
        cout << s << " ";
    }
    cout << endl;
}
```

Sample program p03 dialog.

```
[tt@cs L21]$ p03

Enter a string. One,
One,
Enter a string. two,
One, two,
Enter a string. buckle
One, two, buckle
Enter a string. my
One, two, buckle my
Enter a string. shoe.
One, two, buckle my shoe.
Enter a string.\n
[tt@cs L21]$ 
```
Pattern matching

Regular expressions used to match patterns

Examples

<table>
<thead>
<tr>
<th>Regular Expression</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>/[A-Za-z][A-Za-z\d]/</td>
<td>The first character must be a letter. The second and subsequent characters must be either a letter or a digit.</td>
</tr>
<tr>
<td>/\d+.?\d*</td>
<td>\d+/</td>
</tr>
</tbody>
</table>

6.3.3. String Length Options

<table>
<thead>
<tr>
<th>String Type</th>
<th>Description</th>
</tr>
</thead>
</table>
| static length string | C, Python
The length of the string is fixed during compilation like an array bound. |
| limited dynamic length string | Strings vary up to maximum length that is defined during compilation. |
| dynamic length string | Varying length strings with no maximum similar to the C++ string defined by the class string in the standard C++ library. |

6.3.4. Evaluation

Strings that are implemented as arrays are more cumbersome than strings implemented as a type. When strings are implemented as an array, an assignment must be accomplished via a loop whereas strings implemented as a type have the advantage of assignment implemented via the assignment operator.

6.3.5. Implementation of Character String Types

<table>
<thead>
<tr>
<th>Static string</th>
<th>Length</th>
<th>Address</th>
</tr>
</thead>
<tbody>
<tr>
<td>Limited dynamic string</td>
<td>Maximum length</td>
<td>Current length</td>
</tr>
</tbody>
</table>

Figure 14. Compile-time descriptor for static strings.

Figure 15. Compile-time descriptor for static strings.
6.4. User-Defined Ordinal Types

- An ordinal type is one in which the range of possible value can easily be associated with the set of integers or non-negative integers.
- Primitive ordinal types include
  - integer
  - char
  - Boolean
- User-defined ordinal types include
  - enumeration
  - subrange

6.4.1. Enumeration Types

From C#

```csharp
enum days {sun, mon, tue, wed, thu, fri, sat};
```

Enumeration constants `sun, mon, ..., sat` are names for integer values 0, 1, ..., 6. Enumerated type `days` defines the set of value `sun, mon, ..., sat` and variables of type `days` can take on those values.

Design issues are:
- Is an enumeration constant allowed to appear in more than one type definition, and if so, how is the type of an occurrence of that constant in the program checked?
- Are enumeration values coerced to integer?
- Are any other types coerced to an enumeration type?

6.4.1.1. Designs

<table>
<thead>
<tr>
<th>Language</th>
<th>Declaration and use</th>
</tr>
</thead>
</table>
| Pascal   | `type day = {sun, mon, tue, wed, thu, fri, sat};`  
|          | `var weekday:day;`  
|          | `weekday=wed;`  
|          | `weekday=succ(weekday);`  
|          | `weekday=pred(tue);`  |
| C        | `enum day{sun, mon, tue, wed, thu, fri, sat};`  
|          | `day weekday;`  
|          | `weekday=wed;`  
|          | `weekday=weekday+1;`  
|          | `weekday=tue-1;`  |
| C++      | `enum day{sun, mon, tue, wed, thu, fri, sat};`  
|          | `day weekday;`  
|          | `weekday=wed;`  
|          | `weekday=(day)(weekday+1);`  
|          | `weekday=(day)(tue-1);`  |
6.4.1.2. Evaluation

- Improved **readability** and **reliability**. Named values are easily recognized whereas coded values are not.
- Ada, C#, and Java 5.0 prohibit arithmetic operations on constants and variables having enumeration an enumeration type.
- No enumeration variable can be assigned a value outside its defined range.

6.4.2. Subrange Types

- A **subrange type** is a contiguous subsequence of an ordinal type. For example, 12..14 is a subrange of integer type. Subrange types were introduced by Pascal and are included in Ada.

### 6.4.2.1. Ada’s Design

<table>
<thead>
<tr>
<th>Language</th>
<th>Declaration and use</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pascal</td>
<td><code>type day = (sun,mon,tue,wed,thu,fri,sat);</code> <code>var sick:array[day] of boolean;</code> <code>sick[mon]:=true;</code></td>
</tr>
<tr>
<td>Ada</td>
<td><code>type Days is (Mon, Tue, We, Thu, Fri, Sat, Sun);</code> <code>subtype Weekdays is Days range Mon..Fri;</code> <code>subtype Index is Integer range 1..100;</code></td>
</tr>
</tbody>
</table>

- The compiler must generate range-checking code for every assignment to a subrange variable.

6.4.2.2. Evaluation

- Subrange types enhance readability by making it clear to readers that variables of subtypes can store only certain ranges of values.

6.4.3. Implementation of User-Defined Ordinal Types

- Enumeration types are usually implemented as integers.
- Subrange types are implemented in exactly the same way as their parent types.
- Range checks must be implicitly included by the compiler in every assignment of a variable or expression to a subrange variable.

6.5. Array Types

- An **array** is an aggregate where all the elements usually have the same type.
- Originally, in Fortran, the syntax of an array was made to model that of mathematical subscripts, for example
  
  \[
  \begin{array}{c}
  \text{Mathematical Representation} \\
  a_i \\
  a_{ij} \\
  \end{array}
  \begin{array}{c}
  \text{Typical Array Representation} \\
  a[i] \\
  a[i][j] \\
  \end{array}
  \]

- In many languages, such as C, C++, Java, Ada, and C# all of the elements have the same type.
- In other languages, such as JavaScript, Python, and Ruby, variables are typeless references to objects or data values. In these cases, arrays still consist of elements of a single type, but the elements can reference objects or data values of different types.
6.5.1. Design Issues
Design issues include:
- What types are legal for subscripts?
- Are subscripting expressions in element references range checked?
- When are subscript ranges bound?
- When does array allocation take place?
- Are ragged or rectangular multidimensional arrays allowed, or both?
- Can arrays be initialized when they have their storage allocated?
- What kinds of slices are allowed, if any?

6.5.2. Arrays and Indices
- A reference to an element of an array has two parts:
  - The first part is the name of the array.
  - The second part is the subscript of index.

Examples:

<table>
<thead>
<tr>
<th>Language</th>
<th>Declaration(s)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>C++</td>
<td>double A[9]; int i=5;</td>
<td>A[i]</td>
</tr>
<tr>
<td>Pascal</td>
<td>var A:array[0..9] of real; i:integer; ... i:=5;</td>
<td>A[i]</td>
</tr>
</tbody>
</table>

- A reference to an element in an array can be thought of as a mapping.  
  array_name(subscript_value_list)→element
- The use of parentheses is deliberate: parentheses denote a function in mathematics and functions are characterized using the mapping notation \( f : D \rightarrow R \) meaning function \( f \) is a map from the set \( D \) to the set \( R \). Specific values of \( D, d \in D \) are mapped to set \( R \) by function \( f \) using the notation \( f(d) \).
- Ada retained the mathematical interpretation of arrays and preserved the use of parentheses for arrays. For example:
  \[ Sum:=Sum+B(I); \]
- Designers of other languages like C, C++, and Java specifically elected to distinguish a reference to an array from a reference to a function. Square brackets are used to enclose subscript values.
  \[ Sum:=Sum+B[I]; \]
- A reference to a multidimensional array differs from language to language also.

<table>
<thead>
<tr>
<th>Language</th>
<th>Declaration(s)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>C++</td>
<td>int A[3][5];</td>
<td>for (int r=0;r&lt;3;r++) { for (int c=0;c&lt;5;c++) { A[r][c]=R.Sample(); } }</td>
</tr>
<tr>
<td>Language</td>
<td>Declaration(s)</td>
<td>Reference</td>
</tr>
<tr>
<td>----------</td>
<td>----------------</td>
<td>-----------</td>
</tr>
<tr>
<td>Pascal</td>
<td>type</td>
<td>for $r:=0$ to $2$ do</td>
</tr>
<tr>
<td></td>
<td>imeatrix = array[0..2,0..4] of integer;</td>
<td>begin</td>
</tr>
<tr>
<td></td>
<td>var A: imeatrix;</td>
<td>for $c:=0$ to $4$ do</td>
</tr>
<tr>
<td></td>
<td></td>
<td>begin</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$A[r,c] := \text{random}(100)$;</td>
</tr>
<tr>
<td></td>
<td></td>
<td>end</td>
</tr>
<tr>
<td></td>
<td></td>
<td>end</td>
</tr>
</tbody>
</table>

- Two distinct types are employed to construct an array type.
  - the element type
  - the index type
- The element type can be any type.
- The index type must be an ordinal type that is implemented as an integer.

<table>
<thead>
<tr>
<th>Language</th>
<th>Declaration and use</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pascal</td>
<td>program p03; type</td>
</tr>
<tr>
<td></td>
<td>day_t = (sunday, monday, tuesday, wednesday, thursday, friday, saturday);</td>
</tr>
<tr>
<td></td>
<td>activity_t = (work, play);</td>
</tr>
<tr>
<td></td>
<td>var</td>
</tr>
<tr>
<td></td>
<td>$day$ = array[day_t] of activity_t;</td>
</tr>
<tr>
<td></td>
<td>begin{p03}</td>
</tr>
<tr>
<td></td>
<td>$day[sunday] := \text{play}$;</td>
</tr>
<tr>
<td></td>
<td>$day[monday] := \text{work}$</td>
</tr>
<tr>
<td></td>
<td>end.{p03}</td>
</tr>
</tbody>
</table>

- Ada and Pascal for-loops can use any ordinal type variable for counters.
- Most contemporary languages do not specify range checking of subscripts.
- Java, ML, and C# do specify range checks.
- By default, Ada checks the range of all subscripts.
### 6.5.3. Subscript Bindings and Array Categories

There are five categories of arrays, based on binding to subscript ranges, the binding to storage, and from where the storage is allocated.

<table>
<thead>
<tr>
<th>Category</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>static array</td>
<td>An array in which the subscript ranges are statically bound and storage allocation is static (allocated before run time).</td>
</tr>
<tr>
<td></td>
<td>int A[10]; //A static array</td>
</tr>
<tr>
<td></td>
<td>int main()</td>
</tr>
<tr>
<td></td>
<td>{ return 0;</td>
</tr>
<tr>
<td></td>
<td>}</td>
</tr>
<tr>
<td>fixed stack-dynamic array</td>
<td>An array in which the subscript ranges are statically bound, but the allocation is done at declaration elaboration time during execution.</td>
</tr>
<tr>
<td></td>
<td>void /void)</td>
</tr>
<tr>
<td></td>
<td>{ int A[10]; //A fixed stack-dynamic array</td>
</tr>
<tr>
<td></td>
<td>}</td>
</tr>
<tr>
<td></td>
<td>int main()</td>
</tr>
<tr>
<td></td>
<td>{ f();</td>
</tr>
<tr>
<td></td>
<td>return 0;</td>
</tr>
<tr>
<td></td>
<td>}</td>
</tr>
<tr>
<td>stack-dynamic array</td>
<td>An array in which both the subscript ranges and the storage allocation are dynamically bound at elaboration time.</td>
</tr>
<tr>
<td></td>
<td>void f(int sz)</td>
</tr>
<tr>
<td></td>
<td>{ int A[sz]; //A stack-dynamic array</td>
</tr>
<tr>
<td></td>
<td>}</td>
</tr>
<tr>
<td></td>
<td>int main()</td>
</tr>
<tr>
<td></td>
<td>{ f(25);</td>
</tr>
<tr>
<td></td>
<td>return 0;</td>
</tr>
<tr>
<td></td>
<td>}</td>
</tr>
<tr>
<td>fixed heap-dynamic array</td>
<td>An array in which the subscript ranges and the storage binding are both fixed after storage is allocated.</td>
</tr>
<tr>
<td></td>
<td>void f(int sz)</td>
</tr>
<tr>
<td></td>
<td>{ int* A=new int[sz]; //A fixed heap-dynamic array</td>
</tr>
<tr>
<td></td>
<td>}</td>
</tr>
<tr>
<td></td>
<td>int main()</td>
</tr>
<tr>
<td></td>
<td>{ f(25);</td>
</tr>
<tr>
<td></td>
<td>return 0;</td>
</tr>
<tr>
<td></td>
<td>}</td>
</tr>
<tr>
<td>heap-dynamic array</td>
<td>An array in which the binding of subscript ranges and storage allocation is dynamic and can change any number of times during the array's lifetime.</td>
</tr>
</tbody>
</table>

- C and C++ permit all types of arrays except heap-dynamic arrays.
- Fortran 95 supports fixed heap-dynamic arrays.
- In Java, all arrays are fixed heap-dynamic arrays.
- C# supports heap-dynamic arrays via class ArrayList.
ArrayList intList = new ArrayList();

### 6.5.4. Array Initialization

<table>
<thead>
<tr>
<th>Language</th>
<th>Initialization Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fortran 94</td>
<td>Integer, Dimension (3) :: List = (/0,5,5/)</td>
</tr>
<tr>
<td>C,C++,Java,C#</td>
<td>int[] list = {4,5,7,83};</td>
</tr>
<tr>
<td>C,C++</td>
<td>char* names[] = {&quot;Bob&quot;,&quot;Jake&quot;,&quot;Darcie&quot;};</td>
</tr>
<tr>
<td>Java</td>
<td>String[] names = {&quot;Bob&quot;,&quot;Jake&quot;,&quot;Darcie&quot;};</td>
</tr>
<tr>
<td></td>
<td>//&quot;Bob&quot;,&quot;Jake&quot;, and &quot;Darcie&quot; are references to String objects</td>
</tr>
<tr>
<td>Ada</td>
<td>List: array(1..5) of Integer :=(1,3,5,7,9);</td>
</tr>
<tr>
<td></td>
<td>Bunch: array(1..5) of Integer :=(1 =&gt; 17, 3 =&gt; 34, others =&gt; 0);</td>
</tr>
<tr>
<td>Python</td>
<td>[x*x for x in range(12) if x%3==0]</td>
</tr>
<tr>
<td></td>
<td>produces the array [0,9,36,81]</td>
</tr>
</tbody>
</table>

### 6.5.5. Array Operations

- An array operation is an operation that operates on an array as a unit.
- Common array operations include:
  - assignment
  - catenation
  - equality and inequality comparison
  - slices
- C-based languages do not provide any array operations except through the methods of Java, C++, and C#
- Perl supports array assignment
- Pascal provides array assignment for conformant arrays – for arrays that have the same index values.
- Ada supports array assignment, and catenation (&) where both operands have a single dimension
- Python’s arrays are called lists. Operations on lists include
  - assignment
  - catenation (+)
  - element membership (in)
- Fortran 95 supports array operations called **elemental** because they are between pairs of elements. Elemental operations include:
  - addition (+): The sum of two arrays is an array having the same dimensions where each element in the sum is the sum of corresponding elements in the operands.
  - assignment
  - relational operators
  - arithmetic operators
- Fortran 95 also has libraries having the following operations
  - matrix multiplication
  - matrix transpose
  - vector dot product
- APL: arrays are central to APL
• Addition, subtraction, multiplication, and division are defined for vectors, an array having a single dimension, and matrices.

• Examples
  \(A + B\) //adds scalars, vectors, or matrices
  \(V\) reverses the elements of a Vector.
  \(\Phi M\) reverses the columns of a Matrix.
  \(\Phi M\) reverses the rows of a Matrix.
  \(\phi M\) transposes the Matrix, i.e., the rows become columns and vice versa.
  \(\div M\) inverts the Matrix.

• The . (dot) operator joins selected pairs of operators, for example
  \(+.\times\) for two vectors the combined operator is the dot product
  \(+.\times\) for two matrices the combined operator is matrix multiplication

### 6.5.6. Rectangular and Jagged Arrays

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>rectangular array</td>
<td>A multidimensional array in which all of the rows have the same number of elements, all of the columns have the same number of elements, and so forth. Rectangular arrays model rectangular tables exactly.</td>
</tr>
<tr>
<td>jagged array</td>
<td>An array is which the lengths of the rows need not be the same. For example, a jagged matrix may consist of three rows, one with five elements, one with seven elements, and one with twelve elements. This also applies to the columns and higher dimensions.</td>
</tr>
</tbody>
</table>

• C, C++, and Java support jagged arrays but not rectangular arrays (Your instructor believes, contrary to the text, that C, C++, and Java do support rectangular arrays and that rectangular arrays appear many times more often than jagged arrays.

```java
//A jagged array, I think
int** A=new int*[3];
A[0]=new int[3];
A[1]=new int[5];

//A rectangular array
int A[3][12];
```

• Languages that support jagged arrays employ a separate pair of brackets for each dimension

  \(A[2][7]\)

• Languages that support rectangular arrays define the subscript list to be enclosed in a single pair of square brackets where each subscript is separated by a comma. (Your instructor has an example in Pascal where a reference to an element in a matrix can be appears in both forms, \(A[2][7]\) and \(A[2,7]\). Further, the element reference has no bearing on whether the array is jagged or rectangular.)
A[2,7]

6.5.7. Slices
A slice of an array is some substructure of that array. Examples

<table>
<thead>
<tr>
<th>Example</th>
<th>Explanation</th>
</tr>
</thead>
</table>
| int A[10];
  A[2..7] | Element 2, 3, 4, 5, 6, and 7 of array A. |
| int A[10][10];

- Python supports slices, including entire rows or columns, or consecutively numbered parts of rows or columns. Python also supports more complex slices of arrays including a slice that references every other element of vector.
- Fortran 95 supports complex slices including columns.
- Perl supports slices in two forms, a list of specific subscripts or a range of subscripts.
- Ruby supports slices with the slice method of its Array object.
- Ada supports slices of single dimensioned arrays with consecutive indexes.

6.5.8. Evaluation
- Arrays have been included in virtually all programming languages.
- Advances in arrays since their introduction in FORTRAN have been the inclusion of ordinal types as indexes.
- Newest arrays are associative arrays.

6.5.9. Implementation of Array Types

<table>
<thead>
<tr>
<th>3</th>
<th>4</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>2</td>
<td>5</td>
</tr>
<tr>
<td>1</td>
<td>3</td>
<td>8</td>
</tr>
</tbody>
</table>

- row major order
  3, 4, 7, 6, 2, 5, 1, 3, 8
- column major order
  3, 6, 1, 4, 2, 3, 7, 5, 8

\[
A = \begin{array}{cccccccc}
1 & 2 & \ldots & j-1 & j & \ldots & n \\
1 & & & & & & \\
2 & & & & & & \\
\vdots & & & & & & \\
i-1 & & & & & & \\
i & & & & & & \text{X} \\
\vdots & & & & & & \\
m & & & & & & \\
\end{array}
\]

- location(A[i,j])
  
  \[\text{location}(A[i,j]) = \text{address}(A[1,1]) + (((\# \text{of rows above the } i\text{th row}) \times (\text{size of a row})
  + (\text{number of elements left of the } j\text{th column})) \times \text{element size})\]
• Compile-time descriptors

<table>
<thead>
<tr>
<th>Array Type Descriptor</th>
<th>Integer Type Descriptor</th>
</tr>
</thead>
<tbody>
<tr>
<td>typkind</td>
<td>size</td>
</tr>
<tr>
<td>Typkind</td>
<td>int</td>
</tr>
<tr>
<td>160</td>
<td>64</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Range Type descriptor</th>
<th>Character Type Descriptor</th>
</tr>
</thead>
<tbody>
<tr>
<td>typkind</td>
<td>size</td>
</tr>
<tr>
<td>Typkind</td>
<td>int</td>
</tr>
<tr>
<td>tk_range</td>
<td>8</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Constant Symbol Descriptor</th>
<th>Constant Symbol Descriptor</th>
</tr>
</thead>
<tbody>
<tr>
<td>symkind</td>
<td>identifier</td>
</tr>
<tr>
<td>Symkind</td>
<td>string</td>
</tr>
<tr>
<td>sk_constant</td>
<td>“a”</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Character Type Descriptor</th>
</tr>
</thead>
<tbody>
<tr>
<td>typkind</td>
</tr>
<tr>
<td>Typkind</td>
</tr>
<tr>
<td>tk_character</td>
</tr>
</tbody>
</table>

_type carray=array ['a'..'e'] of integer;_
6.6. Associative Arrays

6.6.1. Structure and Operations

- An associative array is an unordered collection of data elements that are indexed by an equal number of values called keys.
- Perl (called hashes)
  \[
  \%salaries = ("Gary"=>75000,"Perry"=>57000,"Mary"=>55750,"Cedric"=>47850); 
  \]
  \[
  \$s=\$salaries\{"Perry"\}; 
  \]
  \[
  \$s=57000 
  \]
- C++
  \[
  \text{static map\textless string,int\textgreater RW;}
  \]
  \[
  \#define \text{CASE} 260 
  \]
  \[
  RW\["and"]=257; 
  \]
  \[
  RW\["array"]=258; 
  \]
  \[
  RW\["begin"]=259; 
  \]
  \[
  RW\["case"]=\text{CASE}; 
  \]
  \[
  \text{int TokenMgr(int t)} 
  \]
  \[
  \{ 
  \text{int tc=t;}
  \]
  \[
  \text{if (t==IDENTIFIER) \{}
  \]
  \[
  \text{char* s=ToLower(yytext);} 
  \]
  \[
  \text{tc=RW[\text{s}];}
  \]
  \[
  \text{if (tc==0) tc=t;} 
  \]
  \[
  \text{\}}
  \]
  \[
  \text{return tc;}
  \]

6.6.2. Implementing Associative Arrays

- Perl, PHP, C++ - hash

6.7. Record Types

- A record is an aggregate of data elements in which the individual elements are identified by names and accessed through offsets from the beginning of the structure.
- In C, C++, and C# records are supported with the \text{struct} data constructor.
- Design issues that are specific to records include:
  - The syntactic form of references to fields
  - Are elliptical references allowed?

6.7.1. Definition of Records

- The fundamental difference between a record and an array is that a record has elements, or fields, are not referenced by indices. Instead, the fields are named with identifiers, and references to the fields are made using these identifiers.
- (Arrays are aggregates containing elements of the same type whereas records are aggregates containing elements of different types.)
• Aboriginal COBOL
  
  01 EMPLOYEE-RECORD.
  02 EMPLOYEE-NAME.
      05 FIRST PICTURE IS X(20).
      05 MIDDLE PICTURE IS X(10).
      05 LAST PICTURE IS X(20).
  02 HOURLY-RATE PICTURE IS 99V99.

• Pascal
  
  type name_type=array [1..20] of char;
  type employee_name_type = record
      first,middle,last:nametype
  end(employee_name_type);

  type employee_record_type = record
      employee_name:employee_name_type;
      hourly_rate:real
  end(employee_record_type);

  var employee_record:employee_record_type;

  employee_record.first="Thomas         ";
  employee_record.middle="Alva          ";
  employee_record.last="Edison         ";

6.7.2. References to Record Fields

• COBOL – elliptical
  MIDDLE OF EMPLOYEE-NAME OF EMPLOYEE-RECORD
  MIDDLE OF EMPLOYEE-NAME

• Pascal
  
  employee_record(employee_name).first="Thomas    ";
  with employee_record(employee_name) do
    begin
      first="Thomas    ";
      middle="Alva      ";
      last="Edison     ";
    end

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fully qualified reference</td>
<td>A reference in which all intermediate record names, from the largest enclosing record to the specific field, are named in the reference.</td>
</tr>
<tr>
<td>elliptical reference</td>
<td>A reference to the specific field is given but any or all of the enclosing record names can be omitted, as long as the resulting reference is unambiguous.</td>
</tr>
</tbody>
</table>
6.7.3. Operations on Records
- COBOL
  MOVE CORRESPONDING
- C, C++, Java
  field assignment
  record assignment

6.7.4. Evaluation
- Elliptical references allowed COBOL detract from readability
- Both records and arrays describe aggregate data. The difference is that elements of arrays typically share the same type whereas a record is composed of arbitrary types.

6.7.5. Implementation of Record Types
- Fields in records are stored in adjacent memory locations.
- However, data of different types have different sizes and alignment specifications. For example, IEEE 754 Double Binary data occupy 64 bits, or 8 bytes, and are aligned on 8-byte boundaries. Contrast the IEEE 754 Double Binary data to character data that often occupy one byte and are aligned on byte boundaries.

```c
struct example1 {
    char c;
    int i;
    unsigned short s;
    double f;
};
example1 e1;
```

6.8. Tuple Types
A tuple is a data type that is similar to a record, except that the elements are not names.

Python tuple:

```python
myTuple = (3, 5.8, 'apple')
myTuple[1] = 3
```
ML tuple:
```ml
val myTuple = (3, 5.8, 'apple');
```
ML tuples must have at least two elements.
```
#1(myTuple)=3
```

```ml
type intReal = int * real;
```
Values of this type consist of an integer and a real.

```
F#
let tup = (3, 5, 7);;
let a, b, c = tup;;
a=3, b=5, c=7
```

Tuples are used in Python, ML, and F# to allow functions to return multiple values.

### 6.9. List Types

Lists were first supported in the first functional programming language, LISP. They have always been part of the functional languages, but in recent years they have their way into some imperative languages.

List is Scheme and Common LISP are delimited by parentheses and the elements are not separated by any punctuation. For example

```
(A B C D)
```

Nested lists have the same form, so we could have

```
(A (B C) D)
```

Data and code have the same syntactic for in LISP and its descendants. If the list (A B C) is interpreted as code, it is a call to the function A with parameters B and C.

The fundamental list operations in Scheme are two functions that take lists apart and two that build lists. The CAR function returns the first element of its list parameter. For example:

```
(CAR '(A B C))
```

The quote before the parameter list is to prevent the interpreter from considering the list a call to the A function with the parameters B and C, in which case it would interpret it. This call to CAR returns A.

The CDR function returns its parameter list minus its first element. For example, consider

```
(CDR '(A B C))
```

This function call return the list (B C).
In Scheme and Common LISP, new lists are constructed with the CONS and LIST functions. The function CONS takes two parameters and returns a new list with its first parameter as the first element and its second parameter as the remainder of that list. For example, consider the following:

(CONS ‘A ‘(B C))

This call returns the new list (A B C).

The LIST function takes any number of parameters and returns a new list with the parameters as its elements.

(LIST ‘A ‘B ‘(C D))

This call returns the new list (A B (C D))

ML lists [5, 7, 9]
[] – the empty list
CONS in ML is 3 :: [5, 7, 9] resulting in [3, 5, 7, 9]

<table>
<thead>
<tr>
<th>Scheme</th>
<th>ML</th>
</tr>
</thead>
<tbody>
<tr>
<td>CAR</td>
<td>hd (head)</td>
</tr>
<tr>
<td>CDR</td>
<td>tl (tail)</td>
</tr>
</tbody>
</table>

hd [5, 7, 9] is 5
tl [5, 7, 9] is [7, 9]

F# Operations hd and tl are the same, but they are called as methods of the List class as in List.hd [1; 3; 5; 7], which returns 1.

Python has a powerful method for creating arrays called list comprehensions.

[x * x for x in range (12) if x % 3 == 0]

The range function creates the array [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12]

The conditional filters out all numbers in the array that are not evenly divisible by 3.

The expression squares the remaining numbers resulting in the following array.

[0, 9, 36, 81]

6.10. Union Types

- A union is a type whose variables may store different type values at different times during program execution.
- A union is a type whose storage has multiple definitions.

union U {
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In the example above variable c occupies the most significant byte of integer i and floating point variable d.

6.10.1. Design Issues

• A union is a type whose variables may store different type values at different times during program execution.

6.10.2. Discriminated Versus Free Unions

• A free union defines a type where any field in the union may be assigned without validating the field type. This is inherently dangerous because overwriting a part of the storage allocated to a field of a different type will likely destroy that field.

• A discriminated union contains an additional field, called the discriminant, that specifies which of the several types is currently valid.

type Shape = {Circle,Triangle,Rectangle};
type Colour = {Red,Green,Blue};
type Figure = record
    Filled: Boolean;
    Color: Colour;
    case Form: Shape of
        Circle:(Diameter: real);
        Triangle:(Left_Side: integer;Right_Side: integer;Angle: real);
        Rectangle:(Side_1: integer;Side_2: integer);
    end(Figure);
6.10.3. Ada Union Types

```ada
type Shape is (Circle, Triangle, Rectangle);
type Colour is (Red, Green, Blue);
type Figure (Form: Shape) is
record
  Filled: Boolean;
  Color: Colour;
  case Form is
    when Circle =>
      Diameter: Float;
    when Triangle =>
      Left_Side: Integer;
      Right_Side: Integer;
      Angle: Float;
    when Rectangle =>
      Size_1: Integer;
      Size_2: Integer;
  end case;
end record;
```

- A **constrained variant variable** permits static type checking.
  
  ```ada
  Figure_2: Figure(Form => Triangle);
  ```
  
  The constrained variable Figure_2 can only be a triangle and cannot be changed to another variant.

- An **unconstrained variant variable** does not permit static type checking. However, consistency is maintained by allowing only entire records to be assigned. Individual fields may not be assigned in this variant record.
  
  ```ada
  Figure_1: Figure;
  Figure_1:=
    (Filled => True
```
Run-time (dynamic) type checking of variant records detects the error arising from the if-statement below when the Form-tag was assigned the value Circle.

\[
\text{if (Figure_1.Diameter > 3.0) ...}
\]

6.10.4. Evaluation

- Unions are potential unsafe in some languages including Fortran, C, and C++ that are not strongly typed.
- Unions can be safely used in Ada because the design allows for static type checking and, if desired, run-time type checking.
- Java and C# do not permit unions

6.10.5. Implementation of Union Types

\[
\text{type Node (Tag: Boolean) is}

\text{record}

\text{case Tag is}

\text{when True => Count: Integer;}

\text{when False => Sum: Float;}

\text{end case;}

\text{end record;}
\]

6.11. Pointer and Reference Types

- A pointer type is one in which the variables have a range of values that consist of memory addresses and a special value, nil.
- Pointers are used for
  - Indirect addressing
  - Access dynamically allocated storage in a space commonly called a heap.
- Variables that are dynamically allocated from the heap are called heap-dynamic variables. They often do not have identifiers associated with them and thus can be referenced only by pointer or reference type variables. Variables without names are called anonymous variables.
- A pointer variable is distinguished from other types of variables and called a reference type. Other types of variables, including arrays and records, called structured types; and scalar variables are called value types because they store actual values rather than references to values.

6.11.1. Design Issues

- What are the scope and lifetime of a pointer variable?
- What is the lifetime of a heap-dynamic variable?
- Are pointers restricted as to the type of value to which they can point?
• Are pointers used for dynamic storage management, indirect addressing, or both?
• Should the language support pointer types, reference types, or both?

6.11.2. Pointer Operations

• Assignment
  ```
  int* p = new int;
  ```

  ![Figure 6.9.2 Pointer Assignment](image)

• Dereferencing

6.11.3. Pointer Problems

PL/I introduced pointers. PL/I pointers were highly flexible and could point to both heap-dynamic variables and other program variables. To avoid problems with pointers, some newer languages, like Java, have replaced pointers completely with reference types, which, along with implicit deallocation, minimize the primary problems with pointers. A reference type is really only a pointer with restricted operations.

6.11.3.1. Dangling Pointers

A **dangling pointer**, or **dangling reference**, is a pointer that contains the address of a heap-dynamic variable that has been deallocated.

Dangers:
1. The location being pointed to may have been reallocated to some new heap-dynamic variable.
2. If the new variable is not the same type as the old one, type checks of uses of the dangling pointer are invalid.
3. If the dangling pointer is used to change the heap-dynamic variable, the value of the new heap-dynamic variable will be destroyed.
4. It is possible that the location now is being temporarily used by the storage management system, possibly as a pointer in a chain of available blocks of storage, thereby allowing a change to the location to cause the storage manager to fail.

Creating a dangling pointer.
1. A new heap-dynamic variable is created and pointer p1 is set to point at it.
2. Pointer p2 is assigned p1’s value.
3. The heap-dynamic variable pointed to by p1 is explicitly deallocated but p2 is not changed by the operation. p2 is now a dangling pointer.

```c++
int* arrayPtr1;
int* arrayPtr2=new int[100];
arrayPtr1=arrayPtr2;
delete[] arrayPtr2;

//Now, arrayPtr2 is dangling.
```

### 6.11.3.2. Lost Heap-Dynamic Variables

A lost heap-dynamic variable is an allocated heap-dynamic variable that is no longer accessible to the user program. Such variables are often called garbage.

1. Pointer p1 is set to point to a newly created heap-dynamic variable.
2. p1 is later set to point to another newly created heap-dynamic variable.

```c++
int* p1=new int[100];
p1=new int;
//The array created by new int[100] is lost and is now garbage.
```

### 6.11.4. Pointers in Ada

Ada’s pointers are called access types. The dangling-pointer problem is partially alleviated by Ada’s design, at least in theory. A heap-dynamic variable may be (at the implementor’s option) implicitly deallocated at the end of the scope of its pointer type; thus, dramatically lessening the need for explicit deallocation.

However, few if any Ada compilers implement this form of garbage collection, so the advantage is nearly always in theory only.

Unfortunately, the Ada language also has an explicit deallocator, Unchecked_Deallocation. Unchecked_Deallocation can cause dangling pointers.

Lost heap-dynamic variables are not eliminated by Ada’s design.
6.11.5. Pointers in C and C++

In C and C++, pointers can be used in the same ways as addresses are used in assembly languages.

C and C++ permit pointer arithmetic making their use more interesting in those languages compared to languages that do not permit pointer arithmetic.

```c
int* ptr;
int count, init;
...
ptr = &init;   // assign the address of init to ptr
count = *ptr;  // dereference the value stored in variable ptr to refer to the value stored in init. Assign the value in init to count.
```

**Pointer arithmetic in C and C++**

```c
int list[10];
int* ptr;
ptr=list;
  • *(ptr+1) is equivalent to list[1]
  • *(ptr+index) is equivalent to list[index]
  • ptr[index] is equivalent to list[index]
```

C and C++ include pointers of type `void*`, which can point at values of any type.

6.11.6. Reference Types

A reference type variable is similar to a pointer, with one important and fundamental difference: A pointer refers to an address in memory, while a reference refers to an object or value in memory. As a result, although it is natural to perform arithmetic on address, it is not sensible to do arithmetic on references.

C++ includes a special kind of reference type that is used primarily for the formal parameters in function definitions. A C++ reference type variable is a constant pointer that is always implicitly dereferenced.

```c
int result = 0;
int& ref_result = result;
ref_result = 100;
```

In the foregoing code segment `result` and `ref_result` are aliases.

In their quest for increased safety over C++, the designers of Java removed C++-style pointers altogether. Java reference variables can be assigned to refer to different class instances: they are not constants. All Java class instances are referenced by reference variables. That is, in fact, the only use of reference variables in Java.

```java
String str2;
```
str1 = “This is a Java literal string”;

In this code, str1 is defined to be a reference to a String class instance or object. It is initially set to null. The subsequent assignment sets str1 to reference the String object, “This is a Java literal string”.

Because Java class instances are implicitly deallocated, there cannot be dangling references in Java.

C# includes both the references of Java and the pointers of C++.

6.11.7. Evaluation

The problems of dangling pointers and garbage have already been discussed at length.

Pointers have been compared with the goto. The goto statement widens the range of statements that can be executed next. Pointer variables widen the range of memory cells that can be referenced by a variable. Perhaps the most damning statement about pointers was made by Hoare (1973): “Their introduction into high-level languages has been a step backward from which we may never recover.”

6.11.8. Implementation of Pointer and Reference Types

6.11.8.1. Representations of Pointers and References

6.11.8.2. Solutions to the Dangling-Pointer Problem

tombstones
locks-and-keys approach

6.11.8.3. Heap Management

garbage collection
- reference counters
- mark-sweep
- incremental mark-sweep

6.12. Type Checking
compatible
coercion
type error
dynamic type checking

6.13. Strong Typing

6.14. Type Equivalence
Name type equivalence
Structure type equivalence

6.15. Theory and Data Types